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ABSTRACT

Six samples from Holes 417A and 417D, near the southern end of the Bermuda Rise, and one sample (AII-92-29-1) from 23°N Mid-Atlantic Ridge were analyzed for a highly precise determination of REE, Ba, and Sr. As anticipated from theoretical considerations, employment of ordinary linear scale for vertical axis proved strikingly expedient in realizing the comparatively fine but significant characeristics of chondrite-normalized REE patterns of abyssal tholeiites or the like; the Leedey chondrite is employed for normalization.

The abundances of Nd are high for rocks with steeper inclinations for heavy REE (HREE) span. When a regression line is drawn, La and Nd deviate in a negative direction and Ce in a positive direction; there is a correlation between the extents of La deviation and Ce deviation. Moreover, the sum of squares of deviations, ΔLa , ΔCe , and ΔNd , from the regression line for the La-Ce-Nd span increases with the increase of HREE inclination. These observations can be theoretically understood through quantitative study. Meanwhile, it is concluded that the Bermuda Rise rocks correspond to solid-type material system involved with separation from a melt with almost horizontal REE patterns, indicating the F^a value is close to unity. In a relative sense, AII-92-29-1 reflects the separation from melt with a smaller fw. Also, it is worth pointing out that the extensions of regression lines for the Hole 417A and 417D samples intersect the abscissa around $-3.3 \sim -3.4$.

INTRODUCTION

Recently, REE data on abyssal tholeiites have been reported by an increasing number of investigators. An overwhelming majority of abyssal tholeiites show light REE-depleted patterns (Frey and Haskin, 1964; Kay et al., 1970; Schilling, 1971; Kay and Hubbard, 1978), but LREE-enriched patterns have been found (Langmuir et al., 1977; Schilling, 1976; Dostal and Muecke, 1977; Puchelt and Emmermann, 1977; Puchelt et al., 1977), as well as V-shaped ones (Schilling, et al., 1977).

The LREE-depleted REE patterns correspond to those which were designated by Masuda (1966) as solid-type patterns. It is regrettable that those LREE-depleted REE patterns usually are considered as almost identical, and little distinction has been made among them. This is due in part to insufficient accuracies in REE determination. Additionally, this might be attributed to the procedure conventionally employed.

In this introduction, a somewhat detailed explanation will be given to mathematical background developed by one of us (A.M.) for REE pattern analyses and related problems. Masuda (1962) and Coryell et al. (1963) presented a valuable plotting method, in which the logarithms of chondritenormalized values are plotted against the differences in atomic numbers of REE. They emphasized the linearity of patterns resulting from such a plotting procedure. According to mathematical analyses by Masuda and Matsui (1966), such a striking linearity is characteristic of liquid-type materials (Masuda, 1966). The MC plot (named for MasudaCoryell plot) is of essential significance for liquid-type materials. However, it should be kept in mind that, mathematically, the MC plot for solid-type materials is for convenience in distinguishing diagrammatically between liquidtype and solid-type materials, and is less significant than for liquid-type materials.

When the bulk partition coefficient is k, and the residual melt fraction is assumed to be f_w , the ratio of the concentration C_1 in the residual melt relative to the initial concentration C_0 is given by

$$\log C_1/C_0 = -(1 - k) \log f_w$$

The corresponding concentration C_s in the solid surface in equilibrium with the coexisting melt phase should satisfy the relation

$$C_s = k C_1$$

In the above mathematical treatment, equilibrium between the solid surface or forming solid and melt is assumed to hold. Of course, it should be noted that naturally occurring solid-type materials represent systems resulting from accumulation of "solids" in sequential solid-surface equilibrium with diminishing melt phase. A solid-type material can be dealt with as a system which accumulated between two solidification stages corresponding to residual melt fractions, f_w^a and f_w^b (see Appendix), where f_w^a is arbitrarily taken greater than f_w^b . As proved by Masuda and Matsui (1966), the logarithmic linearity of REE pattern of liquid-type material for a span of REE in a MC plot is a reflection of simple linearity of bulk partition coefficients themselves which are responsible for the observed fractionation. This mathematical consideration leads us to a conclusion that, when f_w^a is near unity or a considerably large value, employment of an ordinary linear scale (not a logarithmic scale) as a vertical axis can be essentially significant. (For this reason, Masuda et al. [1977] employed the ordinary linear scale for the vertical axis in their discussions of REE geochemistry of basalt from Ulwan volcano, New Britain.)

We have analyzed six samples from Holes 417A and 417D and one sample (AII-92-29-1) from the Mid-Atlantic Ridge (23°02.63'N/45°01.05'W), for rare-earth elements (REE). This paper is based on the mathematical considerations mentioned above. An ordinary linear scale has been used for the ordinate, which enabled us to distinguish among REE patterns of abyssal tholeiites. It will be shown that highly precise determination of REE and the interpretative viewpoint originating from Masuda (1963) are very valuable and promising.

Bermuda Rise rocks investigated were obtained by drilling near the southern end of the Bermuda Rise; their age is estimated to be older than 100×10^6 yr (Donnelly, Francheteau et al., 1977).

RESULTS

Samples investigated are described in Table 1. Rare-earth elements were determined by mass spectrometric stable isotope dilution technique, with accuracies of better than 1 per cent. However, Gd for Section 417A-41-5 may involve an uncertainty of nearly 2 per cent. The results of determinations of REE, Ba, and Sr are presented in Table 2. For our data presented here, uncertainties in isotope dilution analyses of Ba and Sr are 2 to 3 per cent and 3 to 4 per cent, respectively; these elements were not determined with the same cautions as exercised in REE determination. Major chemical compositions of rocks studied in this report are tabulated in Table 3 (Ui et al., this volume).

DISCUSSION

Comparison of General Patterns Plotted Against a Logarithmic Scale

Figure 1 presents the MC plots where the vertical axis refers to logarithmic scale. In a gross sense, the REE patterns appear to be similar to each other. That is, when the logarithmic ordinate is used for solid-type material, it is often difficult for us to recognize comparatively fine but clearly significant distinctions among solid-type REE patterns. The advantages of ordinary scale over logarithmic scale depend on the values concerned of fw, the procedure of mathematical treatment, and (to a lesser extent) the natures of subjects.

High concentrations of Ba are noted in an altered rock (Section 417A-24-1). For unaltered rocks, the chondritenormalized values are around unity, while the corresponding value for Section 417A-24-1 is about 50, clearly indicating the enhancement of Ba content due to alteration. How-

TABLE 1 Descriptions of Samples Analyzed

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 TABLE 2

 Abundances (ppm) of REE, Ba, and Sr in Rocks Investigated

| - | | | | | | | |
|----|-----------|-----------|-----------|-----------|-----------|-----------|-------------|
| | 417A-24-1 | 417A-41-5 | 417A-44-3 | 417D-22-4 | 417D-32-6 | 417D-45-1 | All-92-29-1 |
| La | 2.68 | 2.08 | 2.40 | 2.20 | 2.22 | 2.41 | 4.12 |
| Ce | 9.44 | 7.01 | 8.13 | 7.52 | 7.44 | 8.56 | 13.36 |
| Nd | 9.79 | 7.42 | 8.65 | 8.01 | 7.88 | 9.15 | 12.59 |
| Sm | 3.58 | 2.75 | 3.21 | 2.92 | 2.95 | 3.42 | 4.30 |
| Eu | 1.259 | 1.028 | 1.201 | 1.124 | 1.127 | 1.279 | 1.550 |
| Gd | 5.01 | 3.95 | 4.71 | 4.29 | 4.31 | 5.01 | 5.93 |
| Dy | 6.01 | 4,94 | 5.81 | 5.38 | 5.39 | 5.96 | 6.94 |
| Er | 3.44 | 3.11 | 3.65 | 3.35 | 3.38 | 3.60 | 4.25 |
| Yb | 3.04 | 3.04 | 3.55 | 3.32 | 3.28 | 3.32 | 4.03 |
| Lu | 0.439 | 0.457 | 0.541 | 0.504 | 0.511 | 0.488 | 0.606 |
| Ba | 225 | 4.96 | | | | 4.22 | 5.55 |
| Sr | 107 | 155 | - | 4 | - | 124 | 138 |

 TABLE 3

 Major Chemical Compositions (after Ui et al., this volume)

| | 417A-24-1 | 417A-41-5 | 417A-44-3 | 417D-22-4 | 417D-32-6 | 417D-45-1 | AII-92-29-1 |
|------------------|-----------|-----------|-----------|-----------|-----------|-----------|-------------|
| SiO ₂ | 48.14 | 48.06 | 48.59 | 46.83 | 47.99 | 46.69 | 48.79 |
| TiO ₂ | 1.47 | 1.35 | 1.52 | 1.38 | 1.46 | 1.68 | 1.81 |
| A1202 | 17.67 | 16.47 | 16.32 | 16.64 | 15.87 | 16.09 | 16.15 |
| FegOa | 7.48 | 4.54 | 4.07 | 4.25 | 3.82 | 4.93 | 2.13 |
| FeÖ | 0.49 | 5.71 | 6.13 | 5.17 | 5.91 | 4.88 | 7.82 |
| MnO | 0.13 | 0.16 | 0.17 | 0.18 | 0.15 | 0.17 | 0.17 |
| MgO | 2.61 | 6.16 | 7.06 | 6.89 | 6.41 | 7.10 | 7.61 |
| CaO | 3.00 | 12.93 | 12.28 | 12.52 | 12.73 | 10.72 | 11.19 |
| NaoO | 1.43 | 2.13 | 2.21 | 2.36 | 2.26 | 2.51 | 2.83 |
| K-O | 6.72 | 0.07 | 0.08 | 0.08 | 0.09 | 0.10 | 0.17 |
| H20+ | 5.79 | 1.66 | 0.80 | 1.92 | 2.04 | 1.93 | 0.78 |
| H-0- | 4.71 | 0.72 | 0.62 | 1.67 | 0.95 | 2.82 | 0.34 |
| P205 | 0.20 | 0.18 | 0.14 | 0.20 | 0.13 | 0.04 | 0.26 |
| Total | 99.84 | 100.14 | 99.99 | 100.09 | 99.81 | 99.66 | 100.05 |

Note: Analysis by H. Haramura.

ever, the REE pattern cannot be judged as affected by alteration. It is true that there is some difference between Section 417A-24-1 and the other two samples from Hole 417A, but this difference can be understood as unrelated with the alteration process. Meanwhile, as seen in Table 2, the Sr content appears totally unaffected by the alteration.

Frey et al. (1974) suggested that the alteration process is accompanied by enrichment of Ba, Sr, and LREE, but their suggestions cannot always be regarded as conclusive, because liquid-type materials seem to be involved therein. Other researchers mention that the alteration process does not change Sr and REE contents (Philpotts et al., 1969; Hart, 1976). Enrichment of Ba by a factor of about 50 without any increase of Sr content as found by us would be the first finding; Hart (1976) reported the double enhancement of Ba content in an altered portion, and Philpotts et al. (1969) observed 50 per cent change of Ba due to alteration.

Comparison of General Patterns Plotted Against an Ordinary Scale

In preparing Figures 2 and 3, ordinary linear scale is employed for vertical axis. Unlike Figure 1, it is easy for us



Figure 1. Chondrite-normalized REE patterns, using a logarithmic scale for the vertical axis.



Figure 2. Chondrite-normalized REE patterns of Hole 417A samples, using an ordinary linear scale for vertical axis, with exhibition of position of intersection with horizontal axis.



Figure 3. Chondrite-normalized REE patterns of Hole 417D samples and AII 92-29-1, using an ordinary linear scale for vertical axis, with exhibition of intersections of lines for 417D samples with horizontal axis.

to detect specific features of REE patterns and recognize their differences. Generally, La, Ce, and Nd appear to plot along a straight line, even though there are small deviations from a strictly linear line. In half of the cases studied, Gd, Dy, Er, Yb, and Lu appear to fall along another straight line. Thus, there appears a sharp break at Gd, while Nd, Sm, and Gd form a curved segment. Of the three samples from Hole 417A, the patterns for Sections 44-3 and 41-5 resemble each other quite well, and the abundance ratios between them reveal small aberrations ranging from +1.5 to -1.8 per cent relative to a mean value, with six of ten elements of REE determined falling within deviations of ± 0.5 per cent. It is also worth pointing out that three lines drawn by the least-square method for La, Ce, and Nd of Hole 417A samples intersect the zero level at substantially the same position on the horizontal axis.

The REE patterns for three Hole 417D samples and AII-92-29-1 are shown in Figure 3 in a similar way as shown in Figure 2. Agreement between Sections 32-6 (massive basalt) and 22-4 (pillow basalt) is remarkably good. Also it is worth mentioning that Sections 32-6 and 22-4 are located above a possible fault zone, while Section 45-1 is from a position below this zone. It is evident that the abyssal tholeiite, AII-92-29-1, is markedly different from the Bermuda Rise rocks.

The positions of intersections of zero level by the extensions of lines drawn by least-square method for La, Ce, and Nd are as follows:

| 417A-24-1 | -3.36 | 417D-22-4 | -3.29 |
|-----------|-------|-------------|-------|
| 417A-41-5 | -3.41 | 417D-32-6 | -3.44 |
| 417A-44-3 | -3.36 | 417D-45-1 | -3.00 |
| | | AII-92-29-1 | -5.10 |

The numerical agreement in intersecting point among Hole 417A samples is in keeping with the observation in Figure 2; the negative values indicate the left-hand position relative to La which is taken, for convenience, as an original point of the horizontal axis. To a lesser extent, convergence of intersection among Hole 417D samples is good.

Attention should be called to the fact that the above values of intersections for Site 417 samples are very close to the corresponding value (-3.3) for a bulk partition coefficient function estimated by Masuda and Matsui (1966) and for an experimentally obtained function (Experiment A of Masuda and Kushiro, 1970). A large absolute value for intersection for AII-92-29-1 would be explained reasonably (Masuda and Shimizu, 1978).

Enlarged Diagrams With Deviations From Partial Regression Lines

Figures 4a, 4b, and 4c are enlarged diagrams for individual samples from Hole 417A. Illustrations at the top exhibit the deviations of each of the REE points from straight lines obtained by application of least-square method



Figure 4a. Enlarged diagram for Section 417A-24-1 (cf. Figure 2), with deviations (%) from regression lines.



Figure 4b. Enlarged diagram for Section 417A-41-5 (cf. Figure 2), with deviations (%) from regression lines.

to more than two points; the absence of a dot for Sm at the top is the result of the least-square method not being applied to a span covering Sm. It will be seen that the deviations for Section 417A-44-3 are within 1.1 per cent, but those for Section 417A-24-1 are much larger (in particular, the La-Ce-Nd span). Figures 5a, 5b, and 5c for Hole 417D samples and Figure 6 for AII are diagrams similar to Figure 4; HREE span for AII-92-29-1 is divided into two segments, Gd-Dy-Er and Er-Yb-Lu. Note that the deviation patterns for La, Ce, and Nd of Section 417D-45-1 and AII-92-29-1 resemble the corresponding one of Sample 417A-24-1.

CONCLUSIONS

It is seen (Figure 7) that the abundances of Nd generally are high for rocks with steeper inclinations for a heavy REE (HREE) span. Specifically, deviations of La, Ce, and Nd from the regression line are of essential significance. It should be noted that Ce deviates in a positive direction, while La and Nd deviate in a negative direction, and that there is a correlation between extents of deviations of La and Ce. This means a convex curvature covering La, Ce, and Nd, and the larger deviation indicates greater curvature. It should be emphatically noted, however, that the curvature under considertion does not contradict the strict linearity of bulk partition coefficients concerned, but mathematically is deduced strictly by assuming the bulk partition coefficients with strict linearity. As seen in Figure 8, the sum of squares of deviations, ΔLa , ΔCe , and ΔNd , from the regression line increases with the increase of HREE inclination, IHRE.

All of these facts are theoretically quite reasonable and can be explained quantitatively. Two curves drawn in Figure 8 are based purely on theoretical calcuations; the two curves correspond to different parameters used in the calculation. Also, Figure 9 demonstrates that a theoretical reinstatement of IHREE to horizontality brings about a kind of covergence of Ism-Gd/INd-Sm, where Ism-Gd and INd-Sm refer to inclinations joining Sm and Gd and Nd and Sm, respectively. For the igneous rocks studied here, the relevant bulk partition coefficients of Nd, Sm, and Gd are regarded nonlinear for this span and such a case is actually observed in Experiment A carried out by Masuda and Kushiro (1970). A detailed explanation of procedures of theoretical calculations will be presented elsewhere (Masuda and Shimizu, 1978).

We conclude that the Bermuda Rise rocks investigated represent the solid-type material systems entangled with high f_w^a values close to unity, whereas the f_w^a value responsible for the genesis of the rock in AII-92-29-1 is estimated to be comparatively small. The high f_w^a values mean the effect of separation from melts with horizontal or almost horizontal REE patterns.

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Figure 4c. Enlarged diagram for Section 417A-44-3 (cf. Figure 2), with deviations (%) from regression lines.

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Figure 5a. Enlarged diagram for Section 417D-22-4 (cf. Figure 3), with deviations (%) from regression lines.

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Figure 5b. Enlarged diagram for Section 417D-32-6 (cf. Figure 3), with deviations (%) from regression lines.

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Figure 5c. Enlarged diagram for Section 417D-45-1 (cf. Figure 3), with deviations (%) from regression lines.



Figure 6. Enlarged diagram for AII 92-29-1 (cf. Figure 3), with deviations (%) from regression lines.



Figure 7. Relationship between Nd content and I_{HREE}.

APPENDIX

Let us consider the concentration, $C_{a,b}^{a,b}$, of a certain rare-earth element in solid-type material system wholly representing solid separated between stages, *a* and *b*, corresponding to residual melt fractions f_w^a and f_w^b . For the above concentration, we have

$$C_{s}^{a,b} = \frac{f_{w}^{a} C_{1}^{a} - f_{w}^{b} C_{1}^{b}}{f_{w}^{a} - f_{w}^{b}}$$
(1)

in which C_1^a and C_1^b are the concentrations in melts at stages *a* and *b*, respectively. Normalizing against initial concentration C₀ gives

$$C_{s}^{a,b}/C_{o} = \frac{f_{w}^{a} (C_{1}^{a}/C_{o}) - f_{w}^{b} (C_{1}^{b}/C_{o})}{f_{w}^{a} - f_{w}^{b}}$$
(2)

Assumption of solidification process with solid-surface equilibrium leads to

$$C_1^a/C_0 = (f_w^a)^{k-1}$$
 (3a)

$$C_1^b/C_o = (f_w^b)^{k-1}$$
 (3b)

where k is a bulk partition coefficient pertaining to the element concerned. Combining Equations 2, 3a, and 3b leads finally to



Figure 8. Relationship between $\Sigma (\Delta x)^2$ (cf. text) and I_{HREE} two curves are theoretically drawn, employing different parameters, independently of observations.



Figure 9. Effect of reinstatement of I_{HREE} to horizontality on I_{Sm-Gd}/I_{Nd-Sm} .

$$C_{s}^{a,b}/C_{o} = \frac{(f_{w}^{a})^{k} - (f_{w}^{b})^{k}}{f_{w}^{a} - f_{w}^{b}}$$
(4)

This general form is highly expedient in theoretical quantitative treatment of solid-type REE patterns. (To avoid probable confusion, it is additionally noted here the k-1 in Equations 3a and 3b and k in Equation 4 work as powers.)